

# Orgoman's Formula Math Destroyer Work Sheet

## Logarithm Rules

$$\log(x \cdot y) = \log(x) + \log(y)$$

$$\log\left(\frac{x}{y}\right) = \log(x) - \log(y)$$

$$\log_a x^b = b * \log_a x$$

$$\log_a x = b \text{ expressed in exponential form is } a^b = x$$

## Exponent Rules

$$a^n \cdot a^k = a^{n+k}$$

$$\frac{a^n}{a^k} = a^{n-k}$$

$$(a^n)^k = a^{n \cdot k}$$

$$a^{-n} = \frac{1}{a^n}$$

$$\sqrt[k]{a^n} = a^{\frac{n}{k}}$$

$$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$$

$$(a \cdot b)^n = a^n \cdot b^n$$

## Conversions

$$K = ^\circ C + 273 \text{ and } ^\circ F = 1.8C + 32$$

$$0^\circ C = 32^\circ F$$

$$1 \text{ inch} = 2.54 \text{ centimeters; } 1 \text{ mile} = 5280 \text{ feet}$$

$$1 \text{ foot} = 12 \text{ inches; } 1 \text{ yard} = 3 \text{ feet}$$

$$1 \text{ meter} \approx 1.1 \text{ yards; } 1 \text{ kilogram} \approx 2.2 \text{ pounds}$$

$$1 \text{ pound} = 16 \text{ ounces} \approx 454 \text{ grams}$$

$$\text{Percent Change} = \frac{(\text{New value} - \text{Old value})}{\text{Old value}} * 100\%$$

# Orgoman's Formula Math Destroyer Work Sheet

How to convert a simple percent word problem to an equation:

'What number' translates to 'x', the unknown.

'is' translates to an equal sign. '='

'of' translates to multiplication

**Example:** What number is 30% of 90?

$$x = \frac{30}{100} \cdot (90)$$

$$x = 0.3 \times 90$$

$$x = 27$$

**Example:** 60 is 40% of what number?

$$60 = \frac{40}{100} * x$$

$$150 = x$$

# Orgoman's Formula Math Destroyer Work Sheet

## Dilutions

$$\% \text{ of pure substance in a mixture} = \frac{\text{Amount of pure substance}}{\text{Total volume of liquid}} \cdot 100\%$$

$$\text{Amount of pure substance mixed} = \% \text{ concentration} \cdot \text{Total Volume of Liquid}$$

## **Distance/Rate**

$$\text{Velocity} = V \quad \text{Distance} = D \quad \text{Time} = T$$

$$D = V \cdot T \quad V = \frac{D}{T} \quad T = \frac{D}{V}$$

When two objects are traveling toward each other, each at its own constant velocity, the rate at which they are approaching each other is the sum of their velocities.

Example: Two cars 180 miles apart are traveling towards each other. Car A is traveling at 60 mph, Car B is traveling at 30 mph. How long will it take them to meet?

$$T = \frac{D}{V}$$

$$\text{Time} = \frac{180}{60+30} = 2 \text{ hours}$$

$$\text{Average speed} = \frac{\text{Total distance}}{\text{Total time}}$$

# Orgoman's Formula Math Destroyer Work Sheet

## Set Operations

$\cup$  = union.  $A \cup B$  is the set of all elements contained in either A or B, that is, the combined elements of each set taken together with duplicates eliminated.

$\cap$  = intersection.  $A \cap B$  is the set of elements that are contained in both A and B.

Example:  $A = \{1,2,3\}$ ,  $B = \{1,3,4\}$

$A \cup B = \{1,2,3,4\}$

$A \cap B = \{1,3\}$

## Simple vs Compounded interest

Simple Interest	Compounded interest
$I = P \cdot r \cdot t$	$I = P \cdot \left(1 + \frac{r}{n}\right)^{n \cdot t}$
P = Principal (initial amount)	P = Principal (initial amount)
I = interest accrued after time t	I = interest accrued after time t
r = rate of interest	r = rate of interest
t = time the money is invested for	t = time the money is invested for
	n = number of times interest is compounded per unit time

Example: If interest is compounded semi-annually (every 6 months), that is,  $n = 2$  times per year, at 3.6 % annual rate. In 4 years ( $t = 4$ ), it will be compounded 8 times. ( $n \cdot t = 2 \cdot 4 = 8$ ).

## Combined Work Problems

Rates are combined when the parties involved are cooperatively working on one and the same project.

[Equation]  $T_1, T_2, T_3, \dots$  represents the time it takes each of the contributing workers to complete the job while working alone. Their respective rates are then  $1/T_1, 1/T_2, 1/T_3, \dots$  etc. The total time T it takes for the entire job to be completed with all contributing workers working simultaneously is given by:

$$\frac{1}{T_1} + \frac{1}{T_2} + \frac{1}{T_3} + \dots = \frac{1}{\text{Total time}}$$

# Orgoman's Formula Math Destroyer Work Sheet

Example: John can paint a Room in 5 hours, Sam can paint the same room in 2.5 hours and Meredith can paint the same room in 3 hours. How long will it take to paint the room if all three work together?

$$\frac{1}{5} + \frac{1}{2.5} + \frac{1}{3} = \frac{1}{T} ; \frac{14}{15} = \frac{1}{T} ; T = \frac{15}{14} \text{ hrs. ; } \frac{15}{14} * 60 \approx 1 \text{ hr and } 4 \text{ mins}$$

## Combinatorics

Combinations and Permutations are used when counting the number of ways to select a subset of objects from a total number of objects.

- Use the combination formula when order does not matter.

For example, {B, C, A}, {A, B, C}, {C, B, A} represent one and the same selection

- Use the permutation formula when order matters.

{B, C, A}, {A, B, C}, {C, B, A} represent three different selections

Out of a total of n things, a subset of r things is considered.

Use the Combination formula,  $nC_r$ , when order does not matter.

$${}_n C_r = \frac{n!}{(n-r)!r!}$$

Use the Permutation formula,  $nP_r$ , when order matters.

$${}_n P_r = \frac{n!}{(n-r)!}$$

# Orgoman's Formula Math Destroyer Work Sheet

## Dice Problems

There are 6 sides to a fair die, numbered 1, 2, 3, 4, 5, 6.

The probability of any one of these outcomes turning out is  $1/6$ .

The sample space of rolling two dice is  $6 \cdot 6 = 36$  possible outcomes.

What is the probability of obtaining a sum of 5 by rolling two dice?

Note that there are 4 ways to roll a sum of 5 with two dice, as follows:

(1, 4), (2, 3), (3, 2), (4, 1).

Since there are only 4 favorable outcomes out of a total of 36 outcomes, the probability of rolling a sum of 5 is:

$$4 \cdot (1/36) = 4/36 = 1/9$$

## Letter Rearrangement Problems

Example: How many ways can the letters in a word "Vermont" be rearranged?

Answer is  $7! = 7 \cdot 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 =$

If there are no repeating letters, the result is  $N!$  where  $N$  is the number of letters in the word.

If repeated letters appear,  $N!$  is then divided by  $a! \cdot b! \cdot c! \cdot \dots$ , etc., where  $a, b, c$ , etc., represents the number of times each letter is repeated.

How many ways can the letters in the word "Accommodate" be rearranged?

Since there are a total of  $N = 11$  letters in the word, with A, C, M and O each appearing twice,

The formula is  $\frac{(\text{Total number of letters})!}{(\text{repeating number of letters})!}$

$$\frac{11!}{2!2!2!2!} = \frac{11 \cdot 10 \cdot 9 \cdot 8 \cdot 7 \cdot 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1}{2 \cdot 1 \cdot 2 \cdot 1 \cdot 2 \cdot 1 \cdot 2 \cdot 1} = 2,494,800$$

# Orgoman's Formula Math Destroyer Work Sheet

## Card Problems

A standard deck consists of:

52 cards (without jokers)

4 suits (hearts, clubs, aces, diamonds)

13 cards per suit

Choosing a card with Replacement: After picking a card, it is put back without changing the total number of cards

Choosing a card without Replacement: After picking a card, one is subtracted from the total number of cards and from the set of cards of interest.

Example: What is the probability of drawing two hearts from a standard deck without replacement?

$$\frac{13}{52} * \frac{12}{51} = 0.24$$

Example: What is the probability of drawing a heart and a spade, in any order, out of a standard deck without replacement?

Solution: Since order is not specified, we must consider two outcomes: heart then spade; spade then heart.

$$\frac{13}{52} * \frac{13}{51} + \frac{13}{52} * \frac{13}{51} = 0.12745$$

## Statistics

[Basic concepts]

**Measures of Central Tendency:** Mean, Median, Mode.

- Mean: the arithmetic average
- Median: the value that divides an ordered dataset in half, such that there are as many numbers greater as there are less than the median value in the dataset.
- Mode: the number that occurs most often in a dataset

**Measures of Dispersion:** Range, Percentile Rank, Standard Deviation, Variance.

These statistics measure the degree to which a dataset is dispersed or spread out on the number line.

- Range: The highest score minus the lowest score in a dataset.

# Orgoman's Formula Math Destroyer Work Sheet

- Percentile Rank: The percent of scores in a dataset that are equal to or less than a given score
- Standard deviation: The established value used to quantify the degree of dispersion or variation of a dataset. See formula below.
- Variance: The square of the standard deviation.

$$\text{Mean of } n \text{ scores } \mu = \sum x_i / n$$

$$\text{Variance } \sigma^2 = \sum (x_i - \mu)^2 / n$$

$$\text{Standard Deviation } \sigma = \sqrt{\sum (x_i - \mu)^2 / n}$$

Notation:

The population mean is represented by the Greek letter mu:  $\mu$

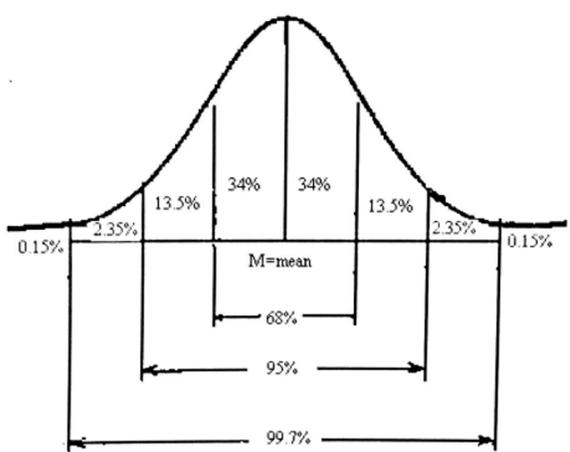
The sum of numbers is represented by the Greek letter, capital sigma:  $\Sigma$

Individual numbers in the set are represented by  $x_i$

The total number of datapoints in the dataset is  $n$

The standard deviation is represented by the Greek letter, small case sigma:  $\sigma$

Empirical Rule, also known as the “68%-95%-99.7% rule”, which says that in a standard normal distribution 68% of the population fall within 1 s.d. of the mean, 95% fall within 2 s.d. of the mean, 99.7% within three s.d. of the mean.



# Orgoman's Formula Math Destroyer Work Sheet

## Geometry

$r$  = radius

$D$  = diameter =  $2r$

Circumference of a circle =  $2\pi r$ , or  $\pi D$

Area of a circle =  $\pi r^2$

Volume of a cylinder =  $\pi r^2 h$ , where  $h$  = height

Surface Area of a cylinder = Lateral area + twice the area of the base  
=  $2\pi r h + 2\pi r^2$  ;

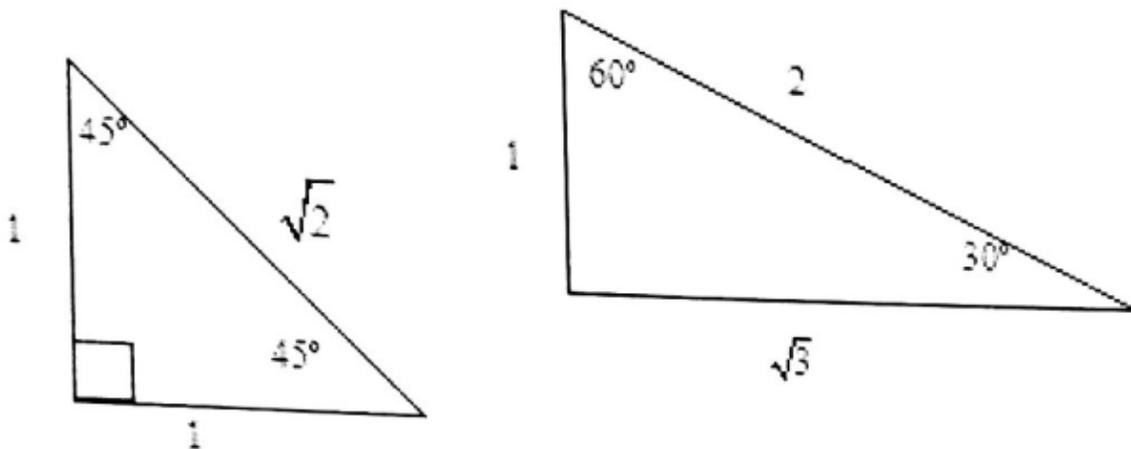
Area of the base of a cylinder =  $\pi r^2$

Volume of a sphere =  $\frac{4}{3}\pi r^3$

Area of a triangle =  $\frac{1}{2}bh$ , where  $b$  = base,  $h$  = height

Area of an equilateral triangle =  $\frac{s^2\sqrt{3}}{4}$  where  $S$  is the side of the triangle

Special Right triangles: the  $45^\circ$ - $45^\circ$ - $90^\circ$  triangle and the  $30^\circ$ - $60^\circ$ - $90^\circ$  triangle. These values are the measures of the angles within each triangle. The sum of the internal angles of a triangle is always  $180^\circ$ .



For the  $30^\circ$ - $60^\circ$ - $90^\circ$  triangle, the ratio of the length of the sides is  $1:\sqrt{3}:2$

For the  $45^\circ$ - $45^\circ$ - $90^\circ$  triangle, the ratio of sides is  $1:1:\sqrt{2}$

# Orgoman's Formula Math Destroyer Work Sheet

## Coordinate Geometry

Equation of a straight line:  $y = mx + b$ ,

where  $m$  = slope and  $b$  is the  $y$ -intercept, located at the point  $(0, b)$

Formula for the slope connecting two points,  $(x_1, y_1)$  and  $(x_2, y_2)$ :

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Formula for the Distance between two points,  $(x_1, y_1)$  and  $(x_2, y_2)$ :

$$D = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

To find the midpoint between two points,  $(x_1, y_1)$  and  $(x_2, y_2)$ :

$$(x_m, y_m) = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

## Quadratic Equations

$$(a + b)^2 = a^2 + 2ab + b^2$$

$$(a - b)^2 = a^2 - 2ab + b^2$$

$$(a - b) \cdot (a + b) = a^2 - b^2$$

## Equations of a Parabola:

General Form:  $F(x) = ax^2 + bx + c$

When  $a > 0$  the parabola is concave up. When  $a < 0$  it is concave down.

The vertex of the parabola is located at  $(x_v, y_d) = \left( -\frac{b}{2a}, F\left(\frac{-b}{2a}\right) \right)$

Standard Form of a parabola:  $F(x) = a(x - h)^2 + k$

Where the vertex is located at  $(h, k)$

# Orgoman's Formula Math Destroyer Work Sheet

Quadratic formula:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Representing the solutions to the Quadratic equation

$$ax^2 + bx + c = 0,$$

Sum of the roots of a quadratic equation:  $\frac{-b}{a}$

Product of the roots of a quadratic equation:  $\frac{c}{a}$